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# Global sea level linked to global temperature

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**We propose a simple relationship linking global sea-level variations on time scales of decades to centuries to global mean temperature. This relationship is tested on synthetic data from a global climate model for the past millennium and the next century. When applied to observed data of sea level and temperature for 1880–2000, and taking into account known anthropogenic hydrologic contributions to sea level, the correlation is >0.99, explaining 98% of the variance. For future global temperature scenarios of the Intergovernmental Panel on Climate Change's Fourth Assessment Report, the relationship projects a sea-level rise ranging from 75 to 190 cm for the period 1990–2100.**

global warming | projections | climate | ocean

Sea-level rise is among the potentially most serious impacts of climate change. But sea-level changes cannot yet be predicted with confidence using models based on physical processes, because the dynamics of ice sheets and glaciers and to a lesser extent that of oceanic heat uptake is not sufficiently understood. This limited understanding is seen, e.g., in the fact that observed sea-level rise exceeded that predicted by models (best estimates) by  $\approx 50\%$  for the periods 1990–2006 (1) and 1961–2003 (2). The last Intergovernmental Panel on Climate Change (IPCC) assessment report did not include rapid ice flow changes in its projected sea-level ranges, arguing that they could not yet be modeled, and consequently did not present an upper limit of the expected rise (2).

This problem has caused considerable recent interest in semiempirical approaches to projecting sea-level rise (3–8). These approaches are based on using an observable that climate models actually can predict with confidence, namely global mean temperature, and establish with the help of observational data how global mean temperature is linked to sea level. A limitation of this approach is that a response that differs fundamentally from that found in the data used cannot be captured, for example, a large and highly nonlinear ice discharge event of a type not in the observational record. This limitation has to be kept in mind when interpreting the results. Here, we present a substantial extension and improvement to the semiempirical method proposed by Rahmstorf (3) (henceforth called R07). We test it on synthetic and real data and apply it to obtain revised sea-level projections up to the year 2100.

## Model

Rahmstorf (3) originally proposed that the initial rate of sea-level rise in response to a large, rapid warming could be approximated by

$$dH/dt = a(T - T_0). \quad [1]$$

Here,  $T_0$  is a base temperature at which sea level is in equilibrium with climate, so that the rate of rise of sea level  $H$ ,  $dH/dt$ , is proportional to the warming above this base temperature.  $T_0$  and  $a$  are to be determined from data. For the ice-melt contribution (glaciers and ice sheets) this approach corresponds to one commonly used in ice modeling, where the rate of mass loss is assumed to be proportional to the temperature increase above a threshold value (9). Some statistical aspects of this work were subsequently challenged (10, 11), but in response the results were

shown to be robust with respect to various choices in the analysis method (12).

Eq. 1 is based on the assumption that the response time scale  $\tau$  of sea level is long compared with the time scale of interest (typically  $\approx 100$  years). Grinsted et al. (8) have recently proposed to model the link of sea level and temperature with a single finite time scale. For the fit to instrumental temperature and sea-level data they obtain a time scale of just over 1,000 years, thus essentially replicating the results of R07, albeit with a different sea-level dataset. However, some components of sea level adjust quickly to a temperature change, e.g., the heat content of the oceanic surface mixed layer. Therefore, we here propose to extend the semiempirical method by a rapid-response term:

$$dH/dt = a(T - T_0) + b dT/dt. \quad [2]$$

This second term corresponds to a sea-level response that can be regarded as “instantaneous” on the time scales under consideration, because it implies  $H \sim T$ . Given the two time scales represented, we will call this the dual model.

## Results

**Testing the Dual Model on Simulated Future Sea-Level Rise.** Testing analysis methods by applying them to model-generated data in addition to those from the real world is a widely used approach. A key advantage of this method is that in the model world, we have complete information and can also analyze future high- $\text{CO}_2$  scenarios. R07 presented a test of his method on future sea-level projections from a coupled climate model (13) and found the method was unable to capture a leveling off of the rate of sea-level rise in the second half of the 21st century found in the climate simulation. We repeat this test with the dual model (Fig. 1). The parameters are fitted to the global temperature and sea-level output from the climate model for 1880–2000, resulting in  $a = 0.080 \pm 0.017 \text{ cm} \cdot \text{K}^{-1} \cdot \text{a}^{-1}$ ,  $b = 2.5 \pm 0.5 \text{ cm} \cdot \text{K}^{-1}$ , and  $T_0 = -0.375 \pm 0.026 \text{ K}$  (temperature relative to the reference period 1951–1980). Sea level for 2000–2100 is then computed from global temperature using Eq. 2 and compared with the sea level simulated by the climate model (which includes a 3D ocean general circulation model) (13). The fact that the rate of rise levels off after 2050 is captured well by the dual model, a circumstance related to temperatures rising less than exponentially. As seen from Eqs. 1 and 2, the dual model is equivalent to the R07 model in case of an exponential temperature increase.

Note that this test is for the thermal expansion component of sea-level rise only, because only that is captured in the climate model. In this case, we expect the rapid response of sea level (second term) to be caused by heat uptake of the surface mixed

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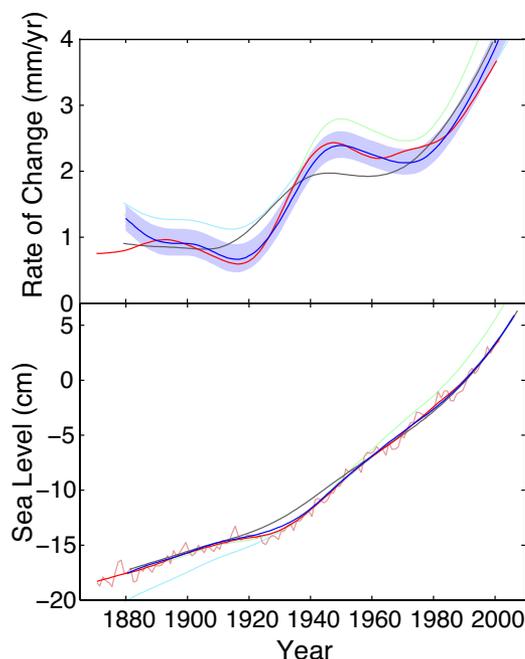
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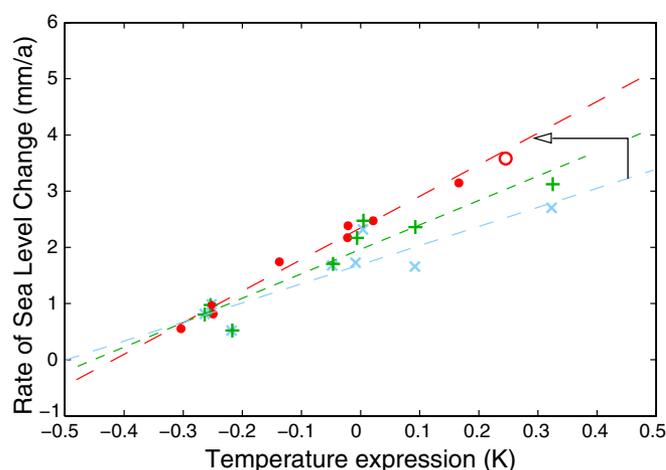


**Fig. 3.** The dual model in the instrumental period. (*Upper*) Observations-based rate of sea-level rise (with tectonic and reservoir effects removed; red) compared with that predicted by Eq. 1 (gray) and Eq. 2 (blue with uncertainty estimate) using observed global mean temperature data. Also shown is the estimate from Eq. 2 using only the first half of the data (green) or the second half of the data (light blue). (*Lower*) The integral of the curves in *Upper*, i.e., sea-level proper. In addition to the smoothed sea level used in the calculations, the annual sea-level values (thin red line) are also shown. The dark blue prediction by Eq. 2 almost obscures the observed sea level because of the close match.

50% for 1993–2003, but with considerable uncertainty. The remainder is mostly caused by ice melt; climate-induced changes in land water storage played a minor, but not negligible, role (15). A recent analysis concludes that during 2003–2008 the split was 20% thermal and 80% ice melt (16). While a 5-year period is likely to be dominated by natural variability, there is some reason for concern that ice melt could take an increasingly larger share in the course of this century.

For temperature we use the National Aeronautics and Space Administration's Goddard Institute for Space Studies dataset (17) because it has the best global coverage. For sea level we use the data of Church and White (18) as adopted by the IPCC. These sea-level data are already corrected for postglacial rebound; because this is a constant linear trend it does not affect our proposed link to temperature. We further corrected the sea-level data for the amount of water stored in manmade reservoirs (see *SI Appendix*), because they cause a small sea-level drop not related to climate that must be excluded from the sea-level changes linked to global temperature as considered in Eq. 2. Possible effects of groundwater mining are considered below.

Fig. 3 shows the remarkably close link of global temperature and the rate of sea-level rise we find for 1880–2000. In particular, it shows that the rate of sea-level rise increased up to 1940 in line with rising temperatures, then stagnated up to the late 1970s while global temperature also remained nearly level, followed by another rise that continues until today. Note that the parameters  $a$  and  $T_0$  are essentially determined by making mean value and trend agree over the data period. Any agreement of the R07 model (Fig. 3, gray line) with observed sea level beyond the linear trend is thus not fitted but an independent test of the



**Fig. 4.** Blue crosses show 15-year averages of global temperature (relative to 1951–1980) versus the rate of sea-level rise, with their linear least-squares fit, as in R07 (3) but using 15-year bins. The green crosses show the adjustment to sea level induced by the reservoir correction (22), leading to a steeper slope. The red dots show the expression  $(T + b/a dT/dt)$  appearing on the right of Eq. 2. This increases the slope again and leads to a much tighter linear fit. The open red circle is a data point based on the satellite altimetry data for 1993–2008. The arrow indicates how the linear trend line changes from that of R07 (blue) to the green one by adjusting the sea-level data (a change along the vertical axis) and then again to the red line by adjusting the temperature expression (along the horizontal axis).

concept. The near-perfect fit of the dual model arises because almost all of the remaining misfit of the R07 model is proportional to  $dT/dt$ .

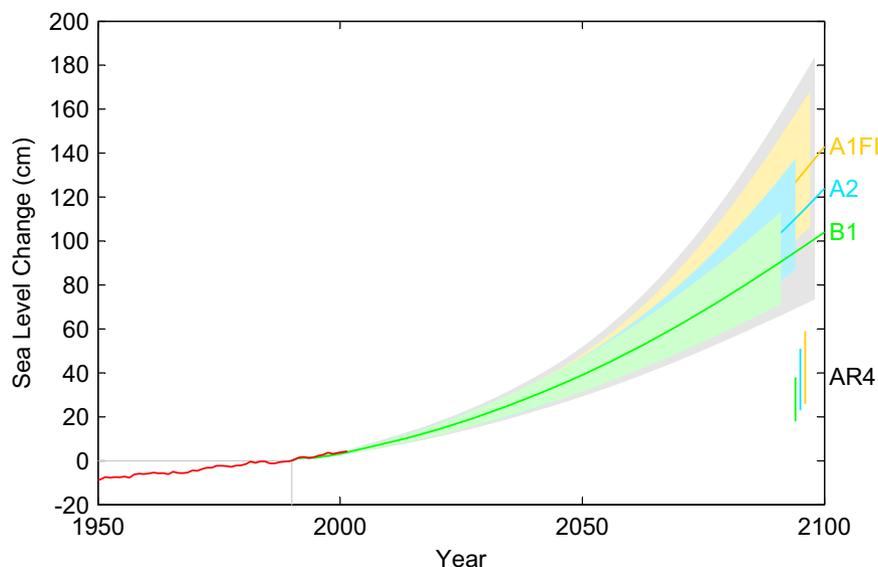
Fig. 4 shows the observations-based rate of sea-level rise as a function of the right sides of Eqs. 1 and 2. The parameter values obtained are  $T_0 = -0.41 \pm 0.03$  K,  $a = 0.56 \pm 0.05$   $\text{cm} \cdot \text{a}^{-1} \cdot \text{K}^{-1}$ , and  $b = -4.9 \pm 1.0$   $\text{cm} \cdot \text{K}^{-1}$ . The linear fit is clearly better for the dual model: the Pearson correlation coefficient  $r = 0.992$  for the dual model (0.96 for the R07 model even when the artificial reservoir correction is applied). This finding is to be expected because the model contains one additional free parameter. Whether it still is the preferred model when this extra degree of freedom is taken into account can be tested with the Akaike information criterion, a standard statistical technique for such cases (see *SI Appendix*). The analysis shows that the dual model is the preferred model, suggesting also here that the second term is physically meaningful.

Another semiindependent test is provided by the satellite sea-level record updated from ref. 16 that started in 1993 and now provides 16 years of data (up including 2008), with a linear trend of 3.4 mm/year (after postglacial rebound adjustment). When the reservoir correction is applied it yields 3.6 mm/year, and the extra point is shown as an open circle in Fig. 4.

Remarkably, the value we find for  $b$  is negative. We can think of two possible physical explanations. The first is that the initial rapid sea-level response to a warming is indeed negative. A possible mechanism for this is higher evaporation from the sea surface and subsequent storage of extra water on land, e.g., in form of soil moisture (19, 20). Note, however, that such a negative effect would have to be large: it would need to compensate the  $b$  of  $+2.5$   $\text{cm} \cdot \text{K}^{-1}$  found earlier for thermal expansion and thus would need to be three times as large as this to cause the overall negative  $b$  value we found. It is hard to see how the very large amount of water needed to be stored on land could remain inconspicuous.

The second possibility is of a positive, but time-lagged, sea-level response. That a negative  $b$  corresponds to a lag is easily seen for the example of a steady linear temperature rise with rate





**Fig. 6.** Projection of sea-level rise from 1990 to 2100, based on IPCC temperature projections for three different emission scenarios (labeled on right, see Projections of Future Sea Level for explanation of uncertainty ranges). The sea-level range projected in the IPCC AR4 (2) for these scenarios is shown for comparison in the bars on the bottom right. Also shown is the observations-based annual global sea-level data (18) (red) including artificial reservoir correction (22).

atures in the various emission scenarios are still close together in the first half of the century. The second term in Eq. 2 furthermore implies a time lag, so that emissions reductions (as in scenario B1) only slow down sea-level rise after more than a decade delay. These results suggest that emissions reductions early in this century will be much more effective in limiting sea-level rise than reductions later on. This effect can be seen when comparing scenarios A1B and A2, which produce the same sea-level rise by 2100 despite A1B being 0.8 °C cooler than. This result is caused by A1B being slightly warmer early on in the 21st century.

Another interesting aspect of these projections is that the thermal share in the rate of sea-level rise declines over the 21st century, if we take the parameters ( $a$ ,  $b$ ) fitted to the climate model simulation above to represent thermal expansion. For the period 1961–2003, the thermal share is  $\approx 30\%$ , as compared with 25% estimated in the AR4 (2) and 40% by Domingues et al. (24). In our projection it gradually declines to  $\approx 20\%$  in the latter half of the 21st century and is directly linked to the fact that thermal expansion is associated with positive  $b$  while total sea level has a negative  $b$ , corresponding to a delay in the ice response. Qualitatively we consider this decline in the thermal share and increasing importance of ice melt a robust result,

which is our key difference to the IPCC AR4 (2), where the ice-melt share is assumed to diminish with thermal expansion contributing between 55% and 70% of the total sea-level rise over the 21st century.

#### Discussion: Implications for the Future

If our method presents a reasonable approximation of the future sea-level response to global warming, then for a given emission scenario sea level will rise approximately three times as much by 2100 as the projections (excluding rapid ice flow dynamics) of the IPCC AR4 (2) have suggested. Even for the lowest emission scenario (B1), sea-level rise is then likely to be  $\approx 1$  m; for the highest, it may even come closer to 2 m.

Uncertainties remain, however. While the thermal expansion response has been tested on simulated data, it is less clear whether the information contained in the 120 years of observational data about the ice response is sufficient to describe the future ice-melt contribution out to the year 2100. The key question then is: will the ice-melt response observed so far, as captured in our dual model, overestimate or underestimate future sea-level rise? On one hand, the surface area of mountain glaciers vulnerable to melting will decrease in future as glaciers disappear. However, more ice higher up in moun-

**Table 1. Temperature ranges and associated sea-level ranges by the year 2100 for different IPCC emission scenarios**

Scenario	Temperature range, °C above 1980–2000	Model average, °C above 1980–2000	Sea-level range, cm above 1990	Model average, cm above 1990
B1	1.4–2.9	2.0	81–131	104
A1T	1.9–3.8	2.6	97–158	124
B2	2.0–3.8	2.7	89–145	114
A1B	2.3–4.3	3.1	97–156	124
A2	2.9–5.3	3.9	98–155	124
A1FI	3.4–6.1	4.6	113–179	143

The temperatures used are taken from the simple model emulation of 19 climate models as shown in figure 10.26 of the IPCC AR4 (2); they represent the mean  $\pm 1$  SD across all models, including carbon cycle uncertainty. The sea-level estimates were produced by using Eq. 2 and 342 temperature scenarios and are given here excluding the uncertainty of the statistical fit, which is approximately  $\pm 7\%$  (1 SD).

tains and particularly the big continental ice sheets will increasingly become subject to melting as temperatures warm. The net effect, an increasing or decreasing surface area subject to melting, is not easily determined without detailed regional studies. In addition, highly nonlinear responses of ice flow may become increasingly important during the 21st century. These are likely to make our linear approach an underestimate. Therefore, we have to entertain the possibility that sea level could rise faster still than suggested by the simple projection based on Eq. 2.

How much faster? Pfeffer et al. (25) provided an independent estimate of maximum ice discharge based on geographic constraints on ice flow; they concluded that sea-level rise in the 21st century is very unlikely to exceed 200 cm. If this estimate is

correct, a nonlinear dynamical ice-sheet response may not change our estimate upward by very much.

To limit global sea-level rise to a maximum of 1 m in the long run (i.e., beyond 2100), as proposed recently as a policy goal (26), deep emissions reductions will be required. Likely they would have to be deeper than those needed to limit global warming to 2 °C, the policy goal now supported by many countries. Our analysis further suggests that emissions reductions need to come early in this century to be effective.

Software code accompanying this article is available ([SI Sea-Level Code](#)).

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